

8.3: Zero and Negative Exponents

Goals: *Simplify expressions raised to the zero power

*Rewrite expressions using all positive exponents

Zero Exponents:

****NOTICE****

$$2^5 =$$

$$5 \cdot 1 = 5$$

and

$$x^m \cdot x^n = x^{m+n}$$

$$2^4 =$$

$$4 \cdot 1 = 4$$

$$b \cdot 1 = b$$

$$x^3 \cdot \underline{\hspace{1cm}} = x^3$$

Anything times 1 is _____!

$$2^3 =$$

$$x^3 \cdot x^? = x^{3+?} = x^3$$

$$2^2 =$$

$$2^1 =$$

$$2^0 = ?$$

1)

2)

****PROOF****

Negative Exponents:

****NOTICE****

$$2^2 =$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$2^1 =$$

$$\frac{2^4}{2^5} = 2^{4-5} = 2^{-1}$$

$$2^0 =$$

$$2^{-1} = \frac{1}{2^?}$$

$$\frac{2 \cdot 2 \cdot 2 \cdot 2}{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2} = \frac{1}{2^?}$$

$$2^{-2} = \frac{1}{2^?}$$

Simplify the following expressions. Write your answer using positive exponents.

Ex: $\left(\frac{2}{3}\right)^0$

Ex: $(-1)^0$

Ex: x^{-2}

Ex: 4^{-3}

Ex: $(-8)^{-2}$

What if the item is already in the denominator and has a negative exponent?

Ex: $\frac{1}{y^{-3}}$

Ex: $\frac{1}{2^{-3}}$

Putting it all together.

Ex: $\frac{7^3}{7^5}$

Ex: $(2xy^{-5})^3$

Ex: $(3x^{-2}y^2)^3$

Ex: $\frac{5^{-1}}{5^2}$

Some more complicated ones:

Ex: $\left(\frac{2}{3}\right)^{-2}$

Ex: $\frac{(2x)^{-2}y^5}{-4x^2y^2}$

Ex: $\frac{4x^{-2}y^4}{8xy^6}$