

### 3.3: Solve Multi-Step Equations

**Goals:** \*Solve multi-step equations by combining like terms  
\*Solve multi-step equations using the distributive property  
\*Solve multi-step equations by multiplying by reciprocals

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#### Steps to Solving Multi-Step Equations

**S** – Simplify

**D** – Distribute

**C** – Combine Like Terms

**B** – Balance using reverse PEMDAS

**A** – Answer

**Combine Like Terms:** Find and combine all like terms on each side of the equals sign separately first

**Ex:**  $8x - 3x - 10 = 20$

$$\begin{array}{r} 5x - 10 = 20 \\ +10 \quad +10 \\ \hline 5x = 30 \\ 5 \quad 5 \\ \hline x = 6 \end{array}$$

**Ex:**  $9x + x - 7 = 13$

$$\begin{array}{r} 10x - 7 = 13 \\ +7 \quad +7 \\ \hline 10x = 20 \\ 10 \quad 10 \\ \hline x = 2 \end{array}$$

**Use the distributive property:** Simplify each side by distributing and combining like terms. Then solve.

**Ex:**  $7x + 2(x + 6) = 39$

$$\begin{array}{r} 7x + 2x + 12 = 39 \\ 9x + 12 = 39 \\ -12 \quad -12 \\ \hline 9x = 27 \\ 9 \quad 9 \\ \hline x = 3 \end{array}$$

**Ex:**  $4x + 3(x - 5) = 6$

$$\begin{array}{r} 4x + 3x - 15 = 6 \\ 7x - 15 = 6 \\ +15 \quad +15 \\ \hline 7x = 21 \\ 7 \quad 7 \\ \hline x = 3 \end{array}$$

**Ex:**  $4x - 7(x - 2) = 26$

$$\begin{aligned} 4x - 7x + 14 &= 26 \\ -3x + 14 &= 26 \\ \underline{-14 \quad -14} & \\ -3x &= 12 \\ \underline{-3 \quad -3} & \\ x &= -4 \end{aligned}$$

**Ex:**  $5x - 4(x - 3) = 17$

$$\begin{aligned} 5x - 4x + 12 &= 17 \\ x + 12 &= 17 \\ \underline{-12 \quad -12} & \\ x &= 5 \end{aligned}$$

### Using Reciprocals:

**Ex:**  $\frac{4}{3} \cdot \frac{3}{4}(z - 6) = 12 \cdot \frac{4}{3}$

$$\begin{aligned} z - 6 &= 16 \\ z &= 22 \end{aligned}$$

**Ex:**  $\frac{2}{3} \cdot \frac{3}{2}(3x + 5) = -24 \cdot \frac{2}{3}$

$$\begin{aligned} 3x + 5 &= -16 \\ 3x &= -21 \\ x &= -7 \end{aligned}$$

**Ex:**  $\frac{5}{2} \cdot \frac{2}{5}(r + 4) = 10 \cdot \frac{5}{2}$

$$\begin{aligned} r + 4 &= 25 \\ r &= 21 \end{aligned}$$

**Ex:**  $-\frac{5}{4} \cdot -\frac{4}{5}(4a - 1) = 28 \cdot -\frac{5}{4}$

$$\begin{aligned} 4a - 1 &= -35 \\ 4a &= -34 \\ a &= -\frac{17}{2} \end{aligned}$$

**Ex:** A flock of cranes migrate from Canada to Texas. The cranes take 14 days (336 hours) and fly at an average speed of 25 miles per hour. They travel a total of 2500 miles. How many hours of migration are the cranes **not** flying?

$$\begin{aligned} d &= rt \\ 2500 &= (25)t \\ 100 &= t \end{aligned}$$

100 hours are spent flying so 236 hours spent **not** flying

