

## Chapter 7: Systems of Equations and Inequalities Study Guide

### 7.1: Solve Systems of Equations by Graphing:

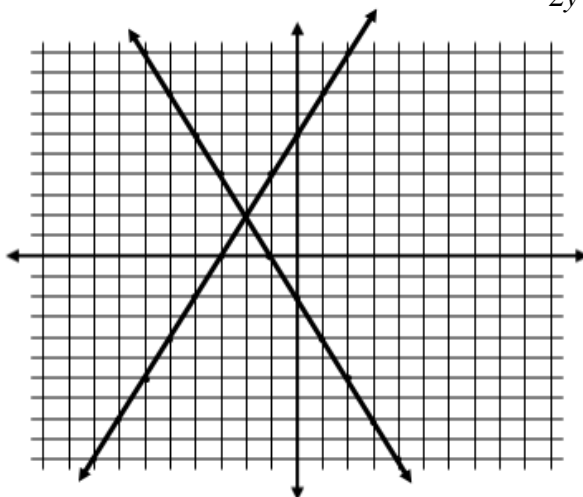
- Be able to identify an ordered pair as a solution to a system

**Ex:** Is (5, 2) a solution to the system:  $2x - 3y = 4$   
 $2x + 8y = 11$

No because if you plug in the ordered pair into **both** equations, it does not work.

- Be able to solve a system of equations by graphing

**Ex:** Solve the system by graphing:  $6x + 3y = -6$   
 $2y - 4x = 12$



### 7.2: Solve Systems of Equations by Substitution:

- Be able to solve a system of equations by substitution

**Ex:**  $y = x - 2$   
 $x = 17 - 4y$

$$\begin{aligned} x &= 17 - 4(x - 2) \\ x &= 17 - 4x + 8 \\ +4x &\quad +4x \\ \hline 5x &= 25 \\ 5 &\quad 5 \\ \hline x &= 5 \end{aligned}$$

$$\begin{aligned} y &= x - 2 \\ y &= 5 - 2 \\ y &= 3 \\ (5, 3) \end{aligned}$$

**Ex:**  $5x + 2y = 9$   
 $x + y = -3$

$$\begin{array}{r} -x \quad -x \\ \hline y = -3 - x \end{array}$$

$$\begin{aligned} 5x + 2(-3 - x) &= 9 \\ 5x - 6 - 2x &= 9 \\ 3x - 6 &= 9 \\ +6 &\quad +6 \\ \hline 3x &= 15 \\ \hline x &= 5 \end{aligned}$$

$$\begin{aligned} y &= -3 - x \\ y &= -3 - 5 \\ y &= -8 \\ (5, -8) \end{aligned}$$

**Ex:**  $y = x - 4$   
 $y = 18 + 2x$

$$\begin{array}{r}
 x - 4 = 18 + 2x \\
 \underline{-x \qquad \qquad -x} \\
 -4 = 18 + x \\
 \underline{-18 \quad -18} \\
 -22 = x \\
 y = x - 4 \\
 y = -22 - 4 \\
 y = -26 \qquad \qquad \qquad (-22, -26)
 \end{array}$$

- Be able to write and solve a linear system

**Ex:** During a football game the parents of football players sell pretzels and popcorn to raise money for new uniforms. They charge \$2.50 for a bag of popcorn and \$2 for a pretzel. The parents collect \$336 in sales during the game and sell twice as many bags of popcorn as pretzels. How many bags of popcorn do they sell? How many pretzels?

Let  $x =$  the number bags of popcorn sold                      Let  $y =$  the number of pretzels sold  
 $2.5x + 2y = 336$                       Popcorn is \$2.50 each, pretzels are \$2. They made \$336 total.  
 $x = 2y$                       There was more popcorn ( $x$ ) sold, so  $y$  needs to be multiplied  
by 2 to make the two amounts equal.

$$\begin{array}{r}
 2.5(2y) + 2y = 336 \\
 5y + 2y = 336 \\
 \underline{7y = 336} \\
 \underline{7 \quad 7} \\
 y = 48
 \end{array}$$

$$\begin{array}{r}
 x = 2y \\
 x = 2(48) \\
 x = 96 \qquad \qquad \qquad 96 \text{ bags of popcorn, } 48 \text{ pretzels}
 \end{array}$$

**7.3 – 7.4: Solve Systems of Equations by Eliminating a Variable:**

- Be able to add or subtract equations to eliminate a variable in order to solve a system

**Ex:**  $4x - 3y = 5$   
 $\underline{+ \quad -2x + 3y = -7}$   
 $\underline{\quad 2x = -2}$   
 $\underline{\quad 2 \quad 2}$   
 $x = -1$

**Ex:**  $6x - 4y = 14$   
 $\underline{- \quad 3x - 4y = 1}$   
 $\underline{\quad 3x = 13}$   
 $\underline{\quad 3 \quad 3}$   
 $x = \frac{13}{3} \text{ or } 4\frac{1}{3}$

After plugging  $x$  into either equation, you would get the value for  $y$ .

$$y = -3$$

$$(-1, -3)$$

$$y = 3$$

$$\left(\frac{13}{3}, 3\right)$$

**Ex:**  $3x + 4y = -6$

$$\underline{2y = 3x + 6}$$

First you have to rewrite the equations so they are lined up. The first equation stays the same, you will subtract  $3x$  in the second equation.

$$\begin{array}{r} 3x + 4y = -6 \\ + \underline{-3x + 2y = 6} \quad \text{Now add the equations together} \\ \hline 6y = 0 \\ 6 \quad 6 \\ y = 0 \quad \text{Plug } y \text{ into either equation to get } x = -2 \\ (-2, 0) \end{array}$$

- Be able to multiply equations first, then eliminate a variable, in order to solve a system

**Ex:**  $x + y = 2$

$$2x + 7y = 9$$

**Ex:**  $4x - 3y = 8$

$$5x - 2y = -11$$

**Multiply the first equation by 2.**  
**Now  $x$  matches.**

$$\begin{array}{r} 2x + 2y = 4 \\ - \underline{2x + 7y = 9} \end{array}$$

Subtract the equations from each other

$$\begin{array}{r} \underline{-5y = -5} \\ -5 \quad -5 \\ y = 1 \end{array}$$

$$\begin{array}{r} x = 1 \\ (1, -1) \end{array}$$

**Multiply the top equation by 2 and multiply the bottom equation by 3.  $Y$  matches now.**

$$\begin{array}{r} 8x - 6y = 16 \\ - \underline{15x - 6y = -33} \end{array}$$

$$\begin{array}{r} \underline{-7x = 49} \\ -7 \quad -7 \\ x = -7 \end{array}$$

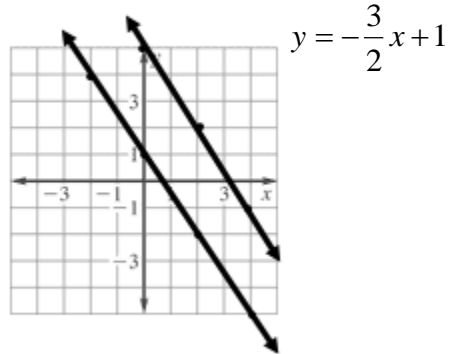
Plug the value of the variable into any equation to find the other value.

$$\begin{array}{r} y = -12 \\ (-7, -12) \end{array}$$

## 7.5: Special Types of Linear Systems:

- Be able to identify when a system of equations has one solution, no solution or an infinite number of solutions by solving using any method.

**Ex:** Solve by graphing:  $3x + 2y = 10$



**No solution, the lines are parallel so they will never intersect.**

**Ex:** Solve by substitution:

$$x - 2y = -4$$

$$y = \frac{1}{2}x + 2$$

**Infinite solutions**

**Ex:** Solve by eliminating:

$$2x - 3y = 6$$

$$2x - 3y = -4$$

**No solution**

- Be able to identify the number of solutions to a system without actually solving it.

**Ex:**  $5x + 3y = 6$

$$-5x - 3y = 3$$

**Ex:**  $y = 2x - 4$

$$-6x + 3y = -12$$

**You must first put both equations in slope-intercept form:**

$$y = -\frac{5}{3}x + 2$$

$$y = -\frac{5}{3}x - 1$$

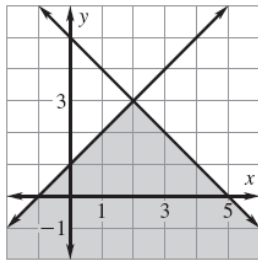
**In the first example, since the slopes are the same and y-intercepts are different, then you can say that the lines are parallel, meaning they will never intersect so there is no solution.**

In the second example, both the slopes and the y-intercepts are the same, so they are the same line, so there is an infinite number of solutions.

**7.6: Solve Systems of Linear Inequalities:**

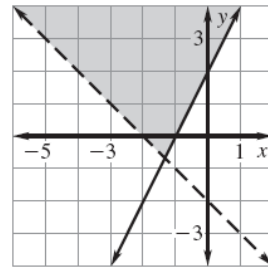
- Be able to identify a solution to a system of linear inequalities

**Ex:** Is (1, 2) a solution?



Yes, it is in the overlapping shaded region.

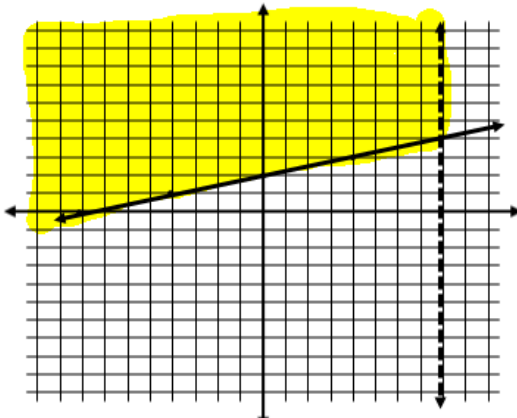
**Ex:** Is (-2, 0) a solution?



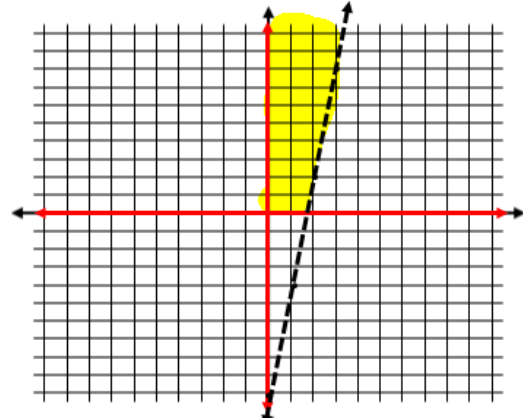
No, its on the dotted line.

- Be able to graph a system of linear inequalities

**Ex:**  $x < 8$   
 $x - 4y \leq -8$

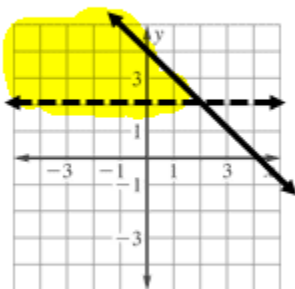


**Ex:**  $x \geq 0$   
 $y \geq 0$   
 $6x - y < 10$

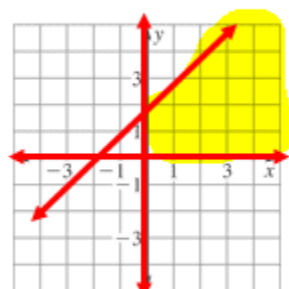


- Be able to write a system of linear inequalities given the graph

**Ex:**



**Ex:**



$$y > 2$$
$$y \leq -x + 4$$

$$y \geq 0$$
$$x \geq 0$$
$$y \leq x + 2$$