## 6.4: Solve Compound Inequalities

Goals: *Translate the verbal phrase into an inequality and graph
*Solve a compound inequality with "and"
*Solve a compound inequality with "or"

## Compound inequalities:

The graph of a compound inequality with "and" is the $\qquad$ of the graphs of the inequalities.

The graph of a compound inequality with "or" is the $\qquad$ of the graphs of the inequalities.

Ex: $\quad x>-2$
Ex: $x \geq 0$

$x \leq 1$

$-2<x$ and $x \leq 1 \rightarrow-2<x \leq 1$


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x<-1 \text { or } x \geq 0
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Translate the verbal phrase into an inequality, then graph the inequality.

Ex: All real numbers that are greater than -2 and less than 3


Ex: All real numbers that are less than 0 or greater than or equal to 2


Ex: All real numbers that are less than -1 or greater than or equal to 4


Ex: All real numbers that are greater than or equal to -3 and less than 5


Ex: All real numbers that are greater than or equal to -4 and less than 4


Ex: All real numbers that are less than -1 or greater than 2


Ex: A crane sits on top of a camera car and faces toward the front. The crane's maximum height is 18 feet and the minimum height is 4 feet. Write and graph a compound inequality that describes the possible heights of the crane.

Ex: At an auction, the lowest bid for an autographed trading card is $\$ 20$. The highest bid is $\$ 54$. Write and graph a compound inequality that describes the possible bids.

## SOLVE a compound inequality with " $\underline{A N D}$ ":

Ex: Solve $2<x+5<9$ and graph your solution. (Hint: Separate into two separate inequalities)

Solve the compound inequalities below:

Ex: $\quad-1<x+1 \leq 7$

Ex: $\quad-7<x-5<4$


Ex: $\quad 10 \leq 2 y+4 \leq 24$

Ex: $\quad-14<x-8<-1$

Ex: $\quad-7<-z-1<3$

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\text { Ex: } \quad-5 \leq-x-3 \leq 2
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Ex: $\quad 1<-2 x+3<19$

Ex: $\quad-1 \leq-5 t+2 \leq 4$


Ex: An investor buys shares of stock and will sell them if the change $c$ in value from the purchase price of a share is less than $-\$ 3.00$ or greater than $\$ 4.50$. Write and graph a compound inequality that describes the changes in value for which the shares will be sold.

## SOLVE a compound inequality with " $\underline{O R}$ ":

Ex: $\quad 2 x+3<9$ or $3 x-6>12$

Ex: $\quad 3 x-2 \leq-11$ or $2 x+8>16$


Ex: $3 h+1<-5$ or $2 h-5>7$


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\text { Ex: } \quad 4 c+1 \leq-3 \text { or } \quad 5 c-3>17
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Ex: The Mars Exploration Rovers Opportunity and Spirit are robots that were sent to Mars in 2003 in order to gather geographical data about the planet. The temperature at the landing sites of the robots can range from $-100^{\circ} \mathrm{C}$ or $0^{\circ} \mathrm{C}$.
a) Write a compound inequality that describes the possible temperatures (in degrees Fahrenheit) at a landing site. (Hint: Use the formula $C=\frac{5}{9}(F-32)$ )
b) Solve the inequality and graph your solution.

c) Identify three possible temperatures (in degrees Fahrenheit) at a landing site.

