

12.4: Simplify Rational Expressions

Goals: *Identify excluded values of rational expressions

*Simplify rational expressions by factoring using the GCF

*Simplify rational expressions by factoring into two binomials

Rational expression:

Excluded values:

Find excluded values for each rational expression:

Ex: $\frac{x+8}{10x}$

Ex: $\frac{5}{2y+14}$

Ex: $\frac{4v}{v^2-9}$

Ex: $\frac{7w+2}{8w^2+w+5}$

Ex: $\frac{x+2}{3x-5}$

Ex: $\frac{2}{5y^2+2y+3}$

Ex: $\frac{n-6}{2n^2-5n-12}$

Ex: $\frac{2m}{m^2-4}$

Simplest Form:

Simplify each rational expression and state the excluded values.

Ex: $\frac{r}{2r}$

Ex: $\frac{5x}{5(x+2)}$

Ex: $\frac{6m^3 - 12m^2}{18m^2}$

Ex: $\frac{y}{7-y}$

Ex: $\frac{4a^3}{22a^6}$

Ex: $\frac{2c}{c+5}$

Ex: $\frac{2s^2 + 8s}{3s + 12}$

Ex: $\frac{8x}{8x^3 + 16x^2}$

Simplify by factoring into binomials and state excluded values:

Ex: $\frac{x^2 - 3x - 10}{x^2 + 6x + 8}$

Ex: $\frac{x^2 + x - 12}{x^2 - x - 6}$

$$\mathbf{Ex:} \frac{x^2 + 3x + 2}{x^2 + 7x + 10}$$

$$\mathbf{Ex:} \frac{y^2 - 64}{y^2 - 16y + 64}$$

Recognize Opposites:

$$\mathbf{Ex:} \frac{x^2 - 7x + 12}{16 - x^2}$$

$$\mathbf{Ex:} \frac{5 + 4z - z^2}{z^2 - 3z - 10}$$

$$\mathbf{Ex:} \frac{x^2 - 7x + 10}{25 - x^2}$$